

The birth of black holes: neutron star collapse times, gamma-ray bursts and fast radio bursts

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ABSTRACT

Recent observations of short gamma-ray bursts (SGRBs) suggest that binary neutron star (NS) mergers can create highly magnetised, millisecond NSs. Sharp cut-offs in *X*-ray afterglow plateaus of some SGRBs hint at the gravitational collapse of these remnant NSs to black holes. The collapse of such ‘supramassive’ NSs also describes the blitzar model, a leading candidate for the progenitors of fast radio bursts (FRBs). The observation of an FRB associated with an SGRB would provide compelling evidence for the blitzar model and the binary NS merger scenario of SGRBs, and lead to interesting constraints on the NS equation of state. We predict the collapse times of supramassive NSs created in binary NS mergers, finding that such stars collapse $\sim 10\text{ s} - 4.4 \times 10^4\text{ s}$ (95% confidence) after the merger. This directly impacts observations targeting NS remnants of binary NS mergers, providing the optimal window for high time resolution radio and *X*-ray follow-up of SGRBs and gravitational wave bursts.

Key words: gamma-ray burst: general — radio continuum: general — stars: magnetars — black hole physics — equation of state

1 INTRODUCTION

Fast radio bursts (FRBs; Lorimer et al. 2007; Keane et al. 2012; Thornton et al. 2013) are among the most exciting astronomical discoveries of the last decade. They are intense, millisecond-duration broadband bursts of radio waves so far detected in the 1.2 GHz to 1.6 GHz band, with dispersion measures between $300\text{ cm}^{-3}\text{ pc}$ and $1200\text{ cm}^{-3}\text{ pc}$. FRBs are not associated with any known astrophysical object. Their anomalously large dispersion measures given their high galactic latitudes, combined with the observed effects of scattering consistent with propagation through a large ionised volume (Lorimer et al. 2007; Thornton et al. 2013), suggest a cosmological origin for FRBs (although, see Burke-Spolaor et al. 2011; Loeb et al. 2014; Bannister & Madsen 2014).

Numerous physical mechanisms have been suggested to produce FRBs at cosmological distances, including magnetar hyperflares (e.g., Popov & Postnov 2013), binary white dwarf (Kashiyama et al. 2013) or neutron star (NS; Totani 2013) mergers, and the collapse of supramassive NSs to form black holes (Falcke & Rezzolla 2013). Here, we focus on the latter mechanism, termed the ‘blitzar’ model. A supra-

massive NS is one that has a mass greater than the non-rotating maximum mass, but is supported from collapse by uniform rotation. As these stars spin down, they lose centrifugal support and eventually collapse to black holes. When magnetic field lines cross the newly-formed horizon, they snap violently, and the resulting outwardly-propagating magnetic shock dissipates as a short, intense radio burst (Falcke & Rezzolla 2013; Dionysopoulou et al. 2013).

The merger of two NSs is one possible formation channel for supramassive NSs. In general, there are three possible outcomes of such a merger, which, for a given NS equation of state (EOS), depend on the nascent NS mass, M_p , and angular momentum distribution. These outcomes are as follows:

(i) If $M_p \leq M_{\text{TOV}}$, where M_{TOV} is the maximum non-rotating mass, the NS will settle to an equilibrium state that is uniformly rotating and eternally stable (e.g., Giacomazzo & Perna 2013).

(ii) If $M_p > M_{\text{TOV}}$, and if magnetic braking has caused the star to rotate uniformly (see below), it will survive for $\gg 1\text{ s}$ as a supramassive star until centrifugal support is reduced to the point where the star collapses to a black hole (e.g., Duez et al. 2006).

(iii) If M_p is greater than the maximum mass that may be supported by uniform rotation, the NS may either instantly

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collapse to a black hole or survive for 10 – 100 ms as a hypermassive star supported by differential rotation and thermal pressures (e.g., Baiotti et al. 2008; Kiuchi et al. 2009; Rezzolla et al. 2011; Hotokezaka et al. 2013).

Gamma-ray bursts (GRBs) with short durations ($\lesssim 2$ s) and hard spectra are associated with the coalescences of compact object binaries, i.e., either NS-NS or NS-black hole mergers (Nakar 2007; Lee & Ramirez-Ruiz 2007; Berger 2013). However, the emission mechanisms of short GRBs (SGRBs) are not well understood. From a theoretical standpoint, a short-lived, collimated, relativistic jet can be launched from both black hole (e.g., Rezzolla et al. 2011) and NS (e.g., Metzger et al. 2008) remnants of compact binary coalescences, as necessitated by the ‘relativistic fireball’ model of prompt GRB emission (e.g., Piran 1999; Nakar 2007; Lee & Ramirez-Ruiz 2007). Jet launching through magnetic acceleration requires a short-lived ($\sim 0.1 - 1$ s) accretion disk, and toroidal and small-opening-angle poloidal magnetic fields that are both $\sim 10^{15}$ G (e.g., Komissarov et al. 2009). Numerical simulations of the merger of two $1.5M_{\odot}$ NSs with 10^{12} G poloidal magnetic fields (Rezzolla et al. 2011) result in a black hole remnant with the necessary conditions, where the magnetic field is amplified through magnetohydrodynamic instabilities, to launch a jet with an energy output of $\sim 1.2 \times 10^{51}$ erg. This is consistent with SGRB observations (Nakar 2007; Lee & Ramirez-Ruiz 2007). Simulations of a lower-mass NS binary coalescence by Giacomazzo & Perna (2013) resulted in a stable millisecond ‘protomagnetar’, although the small-scale instabilities required to amplify the magnetic field to $\sim 10^{15}$ G were unresolved. On the other hand, high-resolution simulations of isolated NSs (e.g., Duez et al. 2006) show that magnetic field amplification to $\sim 10^{15}$ G and accretion disk formation is possible for nascent protomagnetars, suggesting that protomagnetars can power prompt SGRB emission through magnetically accelerated jets. Baryon-free energy deposition through neutrino-antineutrino annihilation, driven by accretion onto protomagnetars, is another mechanism to power prompt SGRBs (Metzger et al. 2008). In this paper, we assume that nascent protomagnetars formed through binary NS coalescences can power prompt SGRB emission, although we note that a deeper understanding is still required.

The most attractive characteristic of the protomagnetar model for SGRBs is its ability to explain features of the X -ray afterglows. Lasting a few hundred seconds following the initial burst, these features are either extremely bright (up to 30 times the fluence of the prompt emission; Perley et al. 2009) and variable on timescales comparable to prompt emission variability, or smoothly decaying plateaus (Rowlinson et al. 2013). Both features are difficult to explain through, for example, fall-back accretion onto black hole central engines (Metzger et al. 2008; Bucciantini et al. 2012, and references therein), although see Siegel et al. (2014). However, the bright X -ray afterglows are explained by the effects of surrounding material on outflows from millisecond protomagnetars with strong magnetic fields (Metzger et al. 2008; Bucciantini et al. 2012). The plateau phases observed in 65% of SGRB X -ray afterglow lightcurves are consistent with electromagnetic spin-down energy losses from protomagnetars with dipolar magnetic field strengths of $B_p > 10^{15}$ G and rotation periods at the beginning of the X -

ray emitting phase of $p_0 \sim 1$ ms (Zhang & Mészáros 2001; Rowlinson et al. 2013). Of this population, 39% show an abrupt decline in X -ray flux within 50–1000 s of the SGRB event, which is interpreted by Rowlinson et al. (2013) as the gravitational collapse of supramassive protomagnetars to black holes. A similar interpretation is given to abrupt declines in the X -ray afterglows of long GRBs (Troja et al. 2007; Lyons et al. 2010).

In this paper, motivated by the possible connection between the protomagnetar model for SGRBs and the blitzar scenario for FRBs (e.g., Zhang 2014), we present a robust estimate of the possible lifetimes of supramassive protomagnetars created in binary NS mergers.¹ The observation of an FRB associated with a sharp decline in the plateau phase of an SGRB X -ray lightcurve would provide powerful evidence for the protomagnetar model for SGRBs, as well as the blitzar model of FRBs. FRB/SGRB associations may also be used to characterise the intergalactic baryon content of the Universe (Deng & Zhang 2014) through measurements of FRB dispersion measures and SGRB redshifts. Our results also provide a quantitative guide to interpreting observations of declines in SGRB X -ray lightcurves (Rowlinson et al. 2013) in the context of supramassive protomagnetar collapse. In particular, secure measurements of the lifetimes of supramassive NSs produced in binary NS mergers allow for interesting new constraints to be placed on the equation of state (EOS) of nuclear matter (Lasky et al. 2014).

Mergers of binary NSs are prime candidate sources for ground-based gravitational wave (GW) interferometers (Abadie et al. 2010). However, the collimated nature of SGRBs (e.g., Burrows et al. 2006) implies not all GW events will be associated with SGRBs. Some alternative electromagnetic signals of GW bursts (Zhang 2013; Gao et al. 2013) rely on the births of stable or supramassive NSs acting as central engines, implying the timescales for these signals are sensitively related to the lifetimes of the nascent NSs and therefore the calculations performed herein.

We show that, if a binary NS merger remnant does not collapse in the first $\sim 4.4 \times 10^4$ s after formation, it is unlikely to collapse at all (97.5% confidence). That is, almost all supramassive NSs born from binary NS mergers will collapse to form black holes within $\sim 4.4 \times 10^4$ s. In §2, we summarise our method for calculating the range of collapse times of merger remnants. We check the consistency of this method against a sample of SGRBs with X -ray plateaus from Rowlinson et al. (2013) in §3. In §4, we generalise our calculations to the full population of binary NS merger remnants, and we present our conclusions in §5.

2 PREDICTING SUPRAMASSIVE NEUTRON STAR COLLAPSE TIMES

The problem of identifying the spin-down torques on nascent NSs has been extensively studied over the last 50 years, with the primary aim of understanding any possible gravitational wave emission (for a review, see Andersson 2003). Two spin-down mechanisms are generally considered: electromagnetic

¹ We stress that FRBs associated with SGRBs are likely to represent only a subset of the FRB population (Zhang 2014).

(EM) radiation driven by the rotating NS magnetic field, and GW emission driven by bar-mode instabilities, stellar oscillation modes or magnetic field deformations. Bar-modes in a rapidly rotating, gravitationally bound fluid body may be excited at large values of $T/|W|$, where T is the rotational kinetic energy and W is the gravitational potential energy. Non-axisymmetric ellipsoids are the only equilibrium configurations for $T/|W| \gtrsim 0.27$ (Chandrasekhar 1969); this limit is reduced to $T/|W| \gtrsim 0.255$ in full General Relativity calculations (Baiotti et al. 2007). For lower values of $T/|W|$, secular instabilities driven either by viscosity (Roberts & Stewartson 1963) or gravitational radiation reaction (the ‘CFS’ instability, Chandrasekhar 1970; Friedman & Schutz 1975) can also lead to the formation of a bar mode. In particular, secular bar modes are excited for $T/|W| \gtrsim 0.14$, where $T/|W| \approx 0.14$ is the bifurcation point between equilibrium sequences of Maclaurin spheroids and the non-axisymmetric Jacobi and Dedekind ellipsoids (see Andersson 2003). The high temperatures of nascent NSs imply low viscosities such that secular bar modes are likely excited through the CFS instability (Lai & Shapiro 1995).

To date, the evolution of supramassive binary NS merger remnants has not been calculated in numerical relativity simulations. Giacomazzo & Perna (2013) showed that a low-mass binary NS merger, with remnant mass $M_p = 2.36M_\odot$, resulted in a stable, differentially rotating, bar-deformed NS within 55 ms. In general, however, if a nascent supramassive NS exhibits a dynamical bar mode, the resulting gravitational radiation will cause the mode to be suppressed on a timescale of $\lesssim 10$ s (e.g., Baiotti et al. 2007; Baiotti et al. 2008; Hotokezaka et al. 2013). Differential rotation within the equilibrium configuration will be suppressed on the Alfvén timescale (Baumgarte et al. 2000; Shapiro 2000), which is approximated as

$$t_{\text{Alfven}} \approx 0.15 \left(\frac{B_p}{10^{15} \text{ G}} \right) \left(\frac{M_p}{M_\odot} \right)^{1/2} \left(\frac{R}{10 \text{ km}} \right)^{-1/2} \text{ s}. \quad (1)$$

For the protomagnetar model of SGRBs under consideration here, $B_p \sim 10^{15}$ G, which suggests that differential rotation is not expected to be significant over timescales $\gg 1$ s. We note, however, that this expression for the Alfvén timescale is likely to be a lower limit given that complex magnetic field structures are expected within protomagnetars (e.g., Giacomazzo & Perna 2013). While dynamical bar-modes excited through shear instabilities may be present for $T/|W| < 0.255$ (Corvino et al. 2010), this mechanism requires significant differential rotation and does not apply on timescales longer than the Alfvén timescale. Hence, for a protomagnetar to survive for $\gg 10$ s, as suggested by SGRB X-ray lightcurve observations (Bucciantini et al. 2012; Rowlinson et al. 2013), it must be truly supramassive, i.e., centrifugally supported against collapse to a black hole by uniform rotation.

We further argue that such a supramassive protomagnetar is unlikely to be subject to the secular bar-mode instability. Throughout this work, we consider three representative EOSs with moderate M_{TOV} that are consistent with current galactic NS observations and the results of Lasky et al. (2014): APR (Akmal et al. 1998, $M_{\text{TOV}} = 2.20 M_\odot$, $R = 10.00$ km, where R is the stellar radius), GM1 (Glendenning & Moszkowski 1991, $2.37 M_\odot$, 12.05 km), and AB-N (Arnett & Bowers 1977, $2.67 M_\odot$, 12.90 km). For each

EOS, we used the general relativistic NS equilibrium code RNS (Stergioulas & Friedman 1995) to generate equilibrium sequences of $T/|W|$ at the Keplerian break-up rotation period p_{Kepler} , assuming uniform rotation. These sequences are plotted against M_p and p_{Kepler} in the left and right panels respectively of Fig. 1. We indicate the values of M_{TOV} for each EOS in the left panel, and also indicate the value of the secular bifurcation point $T/|W| \approx 0.14$ as a horizontal green line in both panels. Only for EOS AB-N are values of $T/|W| > 0.14$ possible, in particular for $M_p \gtrsim M_{\text{TOV}}$. Hence, assuming EOS AB-N, supramassive protomagnetars may develop a secular bar instability. However, the growth timescale of the CFS-driven bar mode instability can be estimated from Lai & Shapiro (1995, their Eq. 2.7). We find a minimum growth time of $\gtrsim 10^6$ s for EOS AB-N which, as we show below, is significantly longer than the maximum lifetime of a supramassive NS for this EOS given EM spin-down alone.

Lasky et al. (2014) calculated the collapse time for a supramassive NS under the assumption of vacuum dipole spin down, showing that this depends on the EOS, the initial magnetic field strength, B_p , the initial spin period, p_0 , and the supramassive NS mass, M_p . The collapse time is given by

$$t_{\text{col}} = \frac{3c^3 I}{4\pi^2 B_p^2 R^6} \left[\left(\frac{M_p - M_{\text{TOV}}}{\alpha M_{\text{TOV}}} \right)^{2/\beta} - p_0^2 \right]. \quad (2)$$

Here, M_{TOV} , R and I are the non-rotating maximum mass, radius and moment of inertia for a given EOS, and α and β define the NS maximum mass as a function of spin period given by $M_{\text{max}}(p) = M_{\text{TOV}} (1 + \alpha p^\beta)$. In Newtonian gravity, $\beta = -2$ and α is determined by the stellar properties. Lasky et al. (2014) calculated general relativistic equilibrium sequences of $M_{\text{max}}(p)$ using RNS (Stergioulas & Friedman 1995) to evaluate α and β for each EOS. For EOS APR, $\alpha = 3.03 \times 10^{-11} \text{ s}^{-\beta}$ and $\beta = -2.95$; EOS GM1 has $\alpha = 1.58 \times 10^{-10} \text{ s}^{-\beta}$ and $\beta = -2.84$; and EOS AB-N has $\alpha = 1.12 \times 10^{-11} \text{ s}^{-\beta}$ and $\beta = -3.22$.

As supramassive protomagnetars born in binary NS mergers are likely to neither be differentially rotating nor losing significant amounts of energy and angular momentum to GWs, we adopt this expression for the collapse time in the present work. We stress, however, that B_p and p_0 for a protomagnetar are taken to be the magnetic dipole strength and spin period respectively at the epoch after which dynamical instabilities and differential rotation are suppressed.

Our assumption of vacuum dipole spin down requires justification. The specific assumption of a dipolar magnetic field structure for binary NS merger remnants is unlikely to be the correct representation. The more pronounced decay with radial distance of high-order multipole components of the field implies that the dipole component will dominate on large spatial scales, and therefore possibly dominate the electromagnetic spin-down. Nonetheless, we emphasise that our calculations in this paper are entirely reliant on this assumption, noting that a magnetic field configuration partitioned into numerous multipoles will result in a slower spin-down rate than a purely dipolar configuration.

Magnetic field induced deformities are not expected to cause significant gravitational wave emission over longer timescales (Haskell et al. 2008). On the other hand, fallback accretion torques may decrease the spin-down (e.g.,

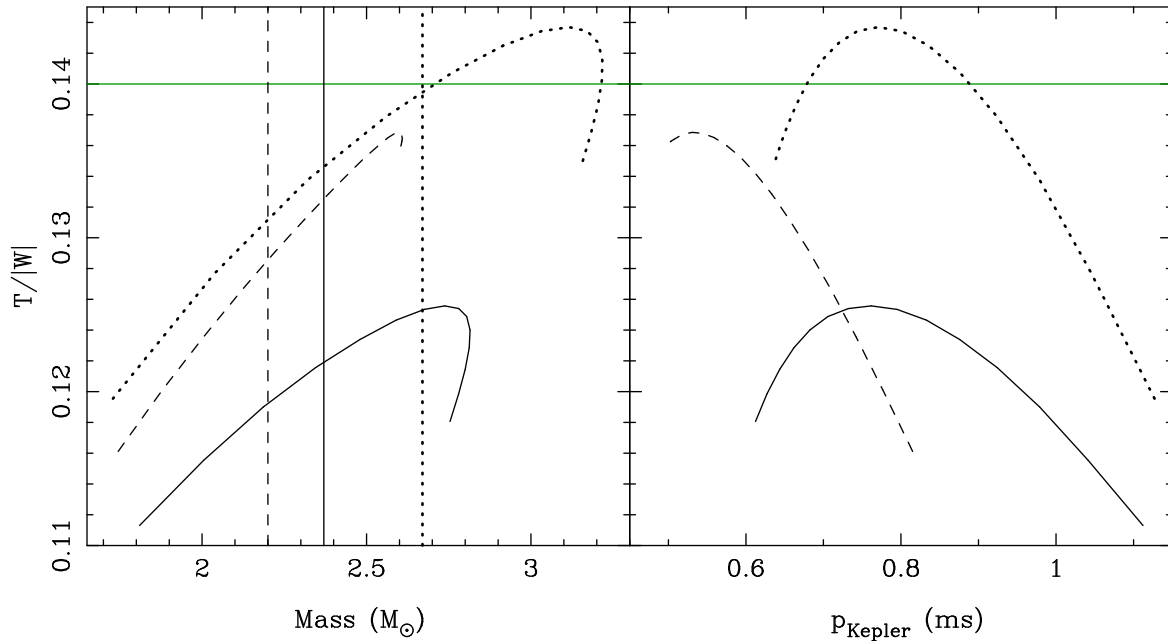


Figure 1. Equilibrium sequences of $T/|W|$ at Keplerian break-up rotation velocity for three EOSs: GM1 (solid curves), APR (dashed curves) and AB-N (dotted curves). We plot $T/|W|$ against the NS mass, M_p , in the left panel, and against p_{Kepler} in the right panel. The vertical lines in the left panel indicate the values of the maximum non-rotating mass, M_{TOV} for each EOS, using the same line styles as the curves. The horizontal green line in both panels at $T/|W| = 0.14$ indicates the approximate value of $T/|W|$ above which NSs are subject to secular instabilities.

Piro & Ott 2011), but the small mass of binary NS merger ejecta (Rezzolla et al. 2011; Hotokezaka et al. 2013; Giacomazzo & Perna 2013) combined with accretion disk heating effects (Bucciantini et al. 2012, and references therein) imply that the accretion torques should be negligible. Finally, while Eq. (2) includes the specific assumption of orthogonal rotation and magnetic axes, we note that $t_{\text{col}} \propto \sin^{-2}(\theta)$, where θ is the angle between the magnetic and rotation axes (Shapiro & Teukolsky 1983). This term introduces a factor of order unity in the collapse time, that we ignore for the remainder of this paper.

The collapse time is strongly dependent on the difference between M_p and $M_{\text{max}}(p)$ for a given EOS. Given a protomagnetar specified by B_p and p_0 , and an EOS which specifies M_{TOV} , R , I , α and β , we use the observationally-derived distribution of NS masses in galactic binary NS systems to predict the distribution of t_{col} . From Kiziltan et al. (2013), $M_{\text{BNS}} \sim N(\mu_{\text{BNS}} = 1.32 M_{\odot}, \sigma_{\text{BNS}} = 0.11)$, where $N(\mu_{\text{BNS}}, \sigma_{\text{BNS}})$ specifies a normal distribution with mean μ_{BNS} and standard deviation σ_{BNS} . Binary NS mergers are believed to approximately conserve rest mass (M_{rest}), with $\lesssim 0.01 M_{\odot}$ of material ejected during the merger (Rezzolla et al. 2011; Hotokezaka et al. 2013; Giacomazzo & Perna 2013). We use the approximate conversion $M_{\text{rest}} = F_{\text{rest}}(M_g) = M_g + 0.075 M_g^2$ (Timmes et al. 1996), where M_g is the gravitational mass, to derive M_p :

$$M_p = F_{\text{rest}}^{-1}[F_{\text{rest}}(M_{\text{BNS}, 1}) + F_{\text{rest}}(M_{\text{BNS}, 2})]. \quad (3)$$

Here, $M_{\text{BNS}, 1, 2}$ are random variables from the distribution $N(\mu_{\text{BNS}}, \sigma_{\text{BNS}})$. By generating a large sample of protomagnetar masses, we produce a large sample of t_{col} trials, allowing us to calculate the cumulative distribution function (CDF), $\hat{f}(t_{\text{col}})$, for the collapse time of a particular protomagnetar assuming a particular EOS.

3 CANDIDATE PROTOMAGNETAR COLLAPSE TIMES

Rowlinson et al. (2013) analysed observations of plateaus in the X-ray lightcurves of SGRBs, fitting protomagnetar spin-down emission models (Zhang & Mészáros 2001) to the data to infer B_p and p_0 . We compare our predictions for the range of possible t_{col} with these observations. We restrict our attention to the sample of eight SGRBs from Rowlinson et al. (2013) that have reliable redshift measurements and show strong evidence for NS central engines [see Table 1 of Lasky et al. (2014)].² Four of these show abrupt declines in their X-ray lightcurves between 90 s and 330 s after the initial GRB, and the remaining four show no departure from the plateau phase for $5 \times 10^4 - 5 \times 10^5$ s, after which the lightcurve is no longer distinguishable from measurement noise.

The four NS candidates that were not observed to collapse will follow one of two evolutionary paths: if $M_p > M_{\text{TOV}}$, the NS will eventually collapse to form a black hole or, if $M_p \leq M_{\text{TOV}}$, the NS will be eternally stable. We calculate CDFs, $\hat{f}(t_{\text{col}})$, for each of these objects using the estimated values of B_p and p_0 from Rowlinson et al. (2013). We reject cases for which $M_p > M_{\text{max}}(p_0)$ as these either instantly collapse to form a black hole or form a dynamically unstable hypermassive NS. We keep track of the number of

² There is debate as to the redshift of GRB 070809. (Rowlinson et al. 2013) fit the NS spin-down model assuming $z = 0.219$ (Perley et al. 2008). While a lower probability host galaxy has been identified at $z = 0.473$ (Berger 2010), we continue to use the Rowlinson et al. (2013) fit in this work, noting that the inferred values of B_p and p_0 change for different redshift identifications.

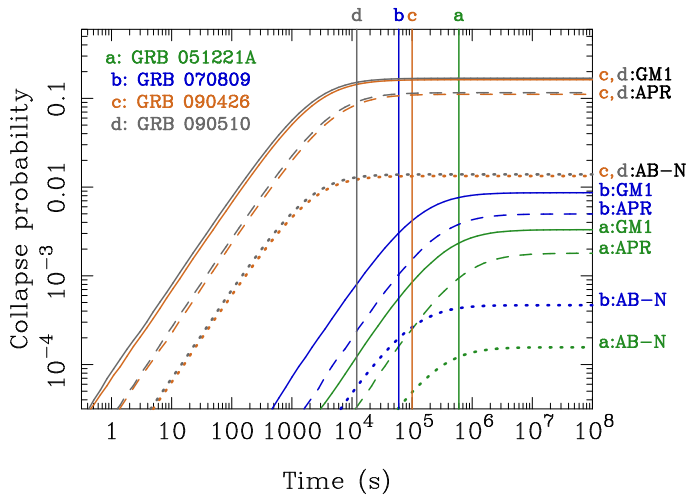


Figure 2. Predicted probability of collapse as a function of time for four protomagnetars in the Rowlinson et al. (2013) sample that are not observed to collapse. The curves indicate the probabilities of $0 < t_{\text{col}} < t$ for a time t after the initial NS-NS mergers. We calculate the probabilities for three EOSs: GM1 (solid curves), APR (dashed curves) and AB-N (dotted curves). The thin vertical lines indicate the (restframe) times of the last observations of the X -ray lightcurves, that in all cases are consistent with the continued existence of the protomagnetars.

cases not included in the samples for which $M_p \leq M_{\text{TOV}}$, in order to appropriately normalise $\hat{f}(t_{\text{col}})$.

In Fig. 2, we plot $\hat{f}(t_{\text{col}})$ for each of the four SGRBs that are not observed to collapse. For each SGRB we consider the three representative EOSs introduced in §2. We do not consider the experimental errors in the determination of B_p and p_0 as they do not significantly affect our results (Lasky et al. 2014). The vertical lines in Fig. 2 are the restframe times of the last observation of the X -ray lightcurves.

The curves in Fig. 2 indicate the probabilities of collapse before a time t after the bursts, i.e., the probabilities of $0 < t_{\text{col}} < t$. Consider GRBs 090426 and 090510 in Fig. 2: if these candidate NSs were born with $M_p > M_{\text{TOV}}$ for any EOS, collapse to a black hole *should* have been observed while the X -ray afterglows were being monitored. Fig. 2 also shows that the probability that these two candidate NSs were born with $M_p \leq M_{\text{TOV}}$ is between 90 – 99% (depending on the EOS) implying stable NSs probably exist in the merger remnants. On the other hand, if the candidate NSs born in GRBs 051221A and 070809 had $M_p > M_{\text{TOV}}$, there is a ~ 30 –60% chance (depending on the EOS and the GRB properties, indicated by the intersections between the relevant curves and vertical lines indicating observation times) that collapse occurred after the observations were concluded rather than during the observations. However, these NSs have a $> 99\%$ chance of having been born with $M_p \leq M_{\text{TOV}}$.

The likelihoods of these four candidate protomagnetars being supramassive, as opposed to eternally stable, are low for all EOSs, which is in agreement with the lack of observational evidence for collapse. It is instructive to consider these likelihoods for the four candidate protomagnetars of Rowlinson et al. (2013), discussed above and in (Lasky et al. 2014), that exhibited sharp declines in their X -ray lightcurves indicative of collapse. For EOS GM1, which

provides the greatest chance of collapse [see also Lasky et al. (2014)], we find a probability for $0 < t_{\text{col}} < \infty$ of 0.2% for the GRB 080905A, 15% for GRB 060801, 18% for GRB 070724A and 60% for GRB 101219A. The latter three predictions are broadly consistent with the Rowlinson et al. (2013) observations.

GRB 080905A is a strange case that has been discussed extensively. Fan et al. (2013) interpreted the slow spin-period (Rowlinson et al. 2013) as evidence that gravitational radiation contributed significantly to the spin-down. However, as discussed in §2, it is difficult to identify a mechanism to generate gravitational radiation on these timescales. It is possible that other issues, such as sub-optimal efficiency of turning rotational energy into electromagnetic energy (Rowlinson et al. 2013) and the inferred redshift (Gruber 2012; Howell & Coward 2013) are also critical. Each of these effects change the inferred values of p_0 and B_p , and hence the probability of collapse.

4 COLLAPSE TIME DISTRIBUTIONS

We now predict the range of possible collapse times, t_{col} , for supramassive stars created in binary NS mergers, using the techniques discussed above for calculating t_{col} for a specific NS and EOS. This requires knowledge of the distributions of p_0 and B_p expected for binary NS merger remnants.

Local, high-resolution numerical simulations indicate that small-scale turbulent dynamos are expected to act throughout a binary NS merger, amplifying internal magnetic fields to $\sim 10^{16}$ G on timescales shorter than the merger timescale (Obergaullinger et al. 2010; Zrake & MacFadyen 2013). Global simulations of binary NS mergers produce similar field strengths through magnetorotational instabilities (e.g., Price & Rosswog 2006; Duez et al. 2006; Siegel et al. 2013), which are consistent with the inferred field strengths from the observations of Rowlinson et al. (2013). We assume all protomagnetars have poloidal magnetic field strengths between 10^{15} G and 3×10^{16} G, where the lower limit is inferred from the need for collimated jets to explain the burst emission (Thompson 2007), and the upper limit is based on magnetic field stability arguments (Metzger et al. 2011).

A supramassive star of mass M_p can have p_0 between the minimum (Keplerian) spin period, p_{Kepler} , and the maximum spin period, p_{max} , that permits the star to remain metastable to collapse. From Eq. (2) the maximum spin period is given by

$$p_{\text{max}} = \left(\frac{M_p - M_{\text{TOV}}}{\alpha M_{\text{TOV}}} \right)^{1/\beta}. \quad (4)$$

We generate random samples of supramassive protomagnetar masses, M_p , for each of the three EOSs we consider, i.e., with $M_{\text{TOV}} < M_p < M_{\text{max}}$. For each mass value, we draw values of p_0 and B_p from log-uniform distributions bounded by $p_{\text{Kepler}} \leq p_0 \leq p_{\text{max}}$ and $1 \leq B_p/10^{15} \text{ G} \leq 30$. Values of p_{Kepler} for each mass value are obtained by cubic interpolation of the equilibrium Keplerian sequences shown in the left panel of Fig. 1, and values of p_{max} are obtained using Eq. (4). We discuss the effects of choosing these distributions below. Having calculated the CDF, $\hat{f}(t_{\text{col}})$, for each sample, we show the estimates of the predictive probability density functions (PDFs) for t_{col} in Fig. 3 for each EOS.

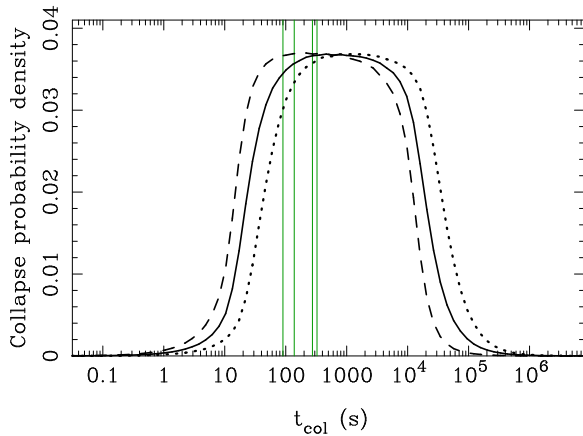


Figure 3. PDFs for t_{col} derived from $\hat{f}(t_{\text{col}})$ for three possible EOSs: GM1 (solid curves), APR (dashed curves) and AB-N (dotted curves). We also show (vertical green lines) the observed values of t_{col} for four SGRB remnants with secure redshift measurements observed to collapse by Rowlinson et al. (2013).

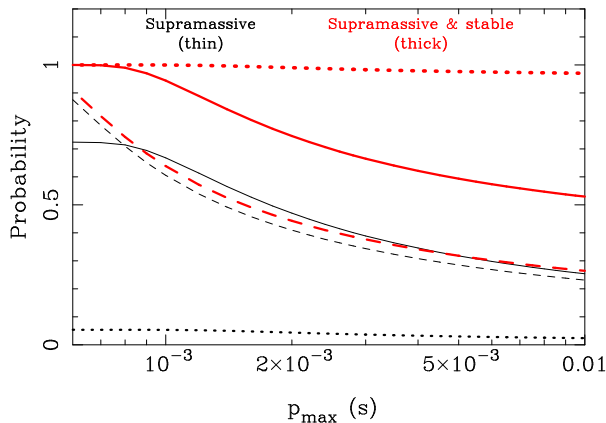


Figure 4. The fraction of binary NS mergers that result in supramassive NSs [i.e., with $M_{\text{TOV}} < M_p < M_{\text{max}}(p_0)$; thin black curves] and supramassive together with eternally stable NSs [$M_p < M_{\text{max}}(p_0)$; thick red curves], as functions of the maximum protomagnetar spin period. The line styles correspond to the different EOSs: GM1 (solid curves), APR (dashed curves) and AB-N (dotted curves).

Fig. 3 shows that the expected collapse times for supramassive protomagnetars formed in binary NS mergers are relatively short. Applying equal weighting to each EOS, we find that t_{col} is in the range $\sim 10 \text{ s} - 4.4 \times 10^4 \text{ s}$ with 95% confidence. The observed restframe collapse times from Rowlinson et al. (2013), shown in Fig. 3 as vertical green lines, are consistent with all EOSs, although they appear somewhat smaller than what may generally be expected.

The PDFs in Fig. 3 encompass a wide range of uncertainties in the collapse times. While we show the effects of the choice of EOS, the PDFs are also affected by uncertainties in M_p , p_0 and B_p . The lower limits of the curves are set by the maximum allowed value of B_p , while the forms of the intrinsic distributions of p_0 and B_p , for which we have assumed the least constraining possibilities, affect the shapes of the curves. Significantly more precise predictions of t_{col} are possible for individual candidate protomagnetars with inferred values of p_0 and B_p . As pointed out in Lasky et al.

(2014), however, the prediction then depends sensitively on the assumed EOS.

We have so far only considered binary NS mergers that result in supramassive stars, i.e., that have $M_{\text{TOV}} < M_p < M_{\text{max}}(p_0)$ and $0 < t_{\text{col}} < \infty$. Of the entire population of binary NS mergers, we find that the probabilities for the newly-created protomagnetars to fall into this category are 5% for EOS AB-N, 72% for EOS GM1 and 97% for EOS APR. Given the sensitivity of these probabilities to the EOS, we *cannot* independently predict the rate of production of supramassive NSs from binary NS mergers.

It is useful to consider how the probabilities of supramassive NS production vary as functions of a universal p_{max} . We note that these probabilities do not depend on the B_p -distribution. In Fig. 4 we repeat our calculations for fixed values of p_{max} , rather than allowing p_{max} to vary depending on M_p for each trial. For each EOS we show two curves: the probability of a binary NS merger resulting in a supramassive NS [i.e., with $M_{\text{TOV}} < M_p < M_{\text{max}}(p_0)$; thin black curves] and the probability of a merger resulting in either a supramassive or an eternally stable NS [i.e., with $M_p < M_{\text{max}}(p_0)$; thick red curves]. We compare the results in Fig. 4 with the observed fractions of SGRBs with X-ray plateaus, and those that also show abrupt declines in X-ray flux (Rowlinson et al. 2013), both of which we consider as upper limits on the true fractions. It is unlikely that EOS AB-N is consistent with the $\sim 40 - 65\%$ of SGRBs observed to have X-ray plateaus (Rowlinson et al. 2013). It is also unlikely that EOS APR is consistent with the $\sim 39\%$ of SGRBs with X-ray plateaus that exhibit abrupt declines. However, EOS GM1 is consistent with both fractions, in particular for $p_{\text{max}} > 8 \text{ ms}$, a result that is also in accordance with the Usov (1992) suggestion that $p_{\text{max}} \sim 10 \text{ ms}$.

5 DISCUSSION AND CONCLUSIONS

We predict the collapse times of supramassive protomagnetars born from the merger of two neutron stars (NSs). We show that, if the protomagnetar has not collapsed within $4.4 \times 10^4 \text{ s}$, the probability that it will ever collapse is small; quantitatively, $P(t_{\text{col}} > 4.4 \times 10^4 \text{ s}) = 0.025$. We also consider the dependence on the assumed NS equation of state (EOS) and the distribution of initial spin periods of the fractions of binary NS mergers that result in supramassive and eternally stable NSs. Of the scenarios we consider, only EOSs similar to GM1 and $p_{\text{max}} > 8 \text{ ms}$ are consistent with the current short gamma-ray burst (SGRB) X-ray lightcurve sample (Rowlinson et al. 2013).

Our results strongly impact observations targeting protomagnetars created in binary NS mergers. We consider these observations in turn:

(i) *Fast radio bursts (FRBs) from blitzars associated with SGRBs.* Falcke & Rezzolla (2013) posit that the collapse of a supramassive NS causes the emission of an intense radio burst. These authors further suggest that $\sim 10^3 \text{ yr}$ may be required to sufficiently clear the NS environments to allow the efficient outward propagation of blitzar radio emission. However, Zhang (2014) found that GRB blast waves and the shocked circum-burst media are likely to have plasma oscillation frequencies significantly lower than FRB emission frequencies, indicating that blitzars occurring shortly

after SGRBs will be visible. Our results show that radio follow-up observations of SGRBs to detect FRBs have an optimal detection window between 10 s and 4.4×10^4 s after the initial burst. This is consistent with the calculation of Zhang (2014), who suggested radio follow-up observations commencing 100 s following the initial burst. We note that from the SGRB sample of Rowlinson et al. (2013), it is likely that between 15% and 25% of SGRBs will result in supramassive stars.

(ii) *X-ray SGRB follow-up*. The theoretical framework that we use to calculate the collapse time window provides a guide to interpreting X-ray observations of SGRBs designed to be sensitive to abrupt declines in plateau phases of the lightcurves. The observation of an abrupt decline greater than 4.4×10^4 s following the initial burst would be inconsistent with this framework.

(iii) *Electromagnetic counterparts to gravitational wave sources*. A large fraction of any non-SGRB signatures of binary NS mergers that rely on a protomagnetar central engine (Zhang 2013; Gao et al. 2013) may have timescales associated with the distribution of supramassive NS collapse times (Fig. 3). Any such signatures with corresponding timescales, conversely, may be suggestive of binary NS mergers.

Our calculations have various uncertainties that require further study. The basic electromagnetic spin down formula we apply to calculate t_{col} in Eq. (2) requires revision to fully model the spin down torques of binary NS merger remnants (Lasky et al. 2014). Additional spin-down mechanisms cause t_{col} to reduce in general, and may affect the overall fractions of supramassive NSs created in binary NS mergers. We also do not account for changes in the gravitational masses, radii and moments of inertia of NSs as they spin down, although these effects are not likely to significantly change our results (e.g., see Falcke & Rezzolla 2013). Our assumption of a simple dipole field structure orthogonally oriented to the rotation axis is also unlikely to be fully correct, although we do not account for this uncertainty in our predictions. The biggest uncertainties included in our predictions of t_{col} come from the assumed distributions for p_0 and B_p and the assumed EOS. We have, however, chosen the broadest possible priors on p_0 and B_p , and consider a variety of EOSs, implying the range of possible t_{col} values we find is conservative.

In conclusion, we strongly urge high time resolution radio and X-ray follow-up observations of short gamma-ray bursts, and in the future gravitational wave bursts, from binary neutron star mergers. The optimal window for these observations is between 10 s and 4.4×10^4 s after the initial bursts. These observations have the potential to provide strong evidence for the protomagnetar model of short gamma-ray bursts and the blitzar model of fast radio bursts.

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